

COMPARISON OF QUANTUM ALGORITHMS FOR QUADRATIC OPTIMIZATION

Monday, 1 December 2025 11:40 (20 minutes)

Optimization problems appear widely in science and industry, yet their classical solutions often demand considerable computational resources. Quantum computing provides a promising framework for addressing such problems more efficiently by exploiting quantum superposition and entanglement [1]. In this work, we investigate several quantum gradient descent [2] approaches to find the minimum of a quadratic cost function. Performing the implementation through Amplitude encoding, we begin by a quantum gradient descent algorithm with a phase estimation-based method. To further enhance performance, we develop and test additional strategies, including linear combination of unitaries (LCUs) [3], the Sz.-Nagy dilation method [4], and a so-called unitary selection method, where the cost function is explicitly defined as a quadratic function. These methods are evaluated in terms of circuit depth, number of iterations, and accuracy. Our results show that the unitary selection outperforms phase estimation, LCUs provide a further improvement, and the Sz.-Nagy approach achieves the highest efficiency among all tested methods. This comparative study highlights the potential of pure quantum algorithms in solving real-world quadratic optimization problems.

[1] Nielsen, M. A., & Chuang, I. L., *Quantum Computation and Quantum Information* (10th Anniversary Edition, 2010), Cambridge University Press.

[2] Rebstroff, P., Schuld, M., Wossnig, L., Petruccione, F., and Lloyd, S., *Quantum gradient descent and Newton's method for constrained polynomial optimization*, *New J. Phys.*, 21(7):073023, (2019).

[3] Chakraborty, Shantanav. "Implementing any linear combination of unitaries on intermediate-term quantum computers." *Quantum* 8 (2024): 1496.

[4] Gaikwad, Akshay, Arvind, and Kavita Dorai. "Simulating open quantum dynamics on an NMR quantum processor using the Sz.-Nagy dilation algorithm." *Physical Review A* 106.2 (2022): 022424.

Presenting Author

Helarie Rose Medie Fah

Email

223153323@stu.ukzn.ac.za

Student or Postdoc?

PhD or DTech

Institute

University of KwaZulu Natal

Registered for the conference?

Yes

CHPC User

CHPC Research Programme

Primary author: Ms FAH , Helarie Rose Medie (UKZN)

Presenter: Ms FAH , Helarie Rose Medie (UKZN)

Session Classification: Special

Track Classification: Quantum Computing